PGDM (IB), 2013 -15 Statistics for Business Analysis IB-104

Trimester - I, End-Term Examination: September 2013

Time allowed: 2 hrs 30 min

Roll N	10.	
LOUI I	10	

Instruction: Students are required to write Roll No on every page of the question paper, writing anything except the Roll No will be treated as **Unfair Means**. In case of rough work please use answer sheet.

SECTION A

Attempt ANY three questions in this section. Each question carries 5 marks. (3 X 5)

- A1. The mean number of hours of flying time for pilots at Continental Airlines is 49 hours per month. Assume that this mean was based on actual flying times for a sample of 100 Continental pilots and that the sample standard deviation was 8.5 hours.
 - a. At 95% confidence what is the margin error?
 - b. What is the 95% confidence interval estimate of the population mean flying time for the pilots?
- A2. The average number of customers, who appear at a counter of a certain bank per minute, is two. Find the probability that during a given minute
 - a. No customer appears
 - b. Three or more customer appear (Given e-2 = 0.1353)
- A3. List the reasons for sampling. Explain two methods of probability sampling with appropriate examples in market research.
- A4. According to a survey, 48% of executives believe that employees are most productive on Tuesday. Suppose 200 executives are randomly surveyed:
- a. what is the probability that fewer than 90 of the executives believe employees are most productive on Tuesdays.
- b. What is the probability that more than 100 of the executives believe employees are most productive on Tuesdays.
- A5. Complete the One-Way ANOVA summary table at a 0.05 level of significance.

Source	SS	df	MS	F	
Between (group)	80		40	s	
Within/Error			-		
Total	100	14			

SECTION B

Attempt ANY two questions in this section. Each question carries 10 marks.

(2 X 10)

B1. Last year, five randomly selected students took a math aptitude test before they began their statistics course.

Student	Scores on aptitude test	Statistical grades
1	95	85
2	85	95
3	80	70
4	70	65
5	60	70

The Statistics Department has four questions.

- a. What linear regression equation best predicts statistics performance, based on math aptitude scores?
- b. If a student made an 80 on the aptitude test, what grade would we expect her to make in statistics?
- c. How well does the regression equation fit the data?, (Calculate R²)
- d. Calculate the correlation coefficient between score on aptitude test and statistical grades scored by the students.
- B2. According to the 1994 World Almanac the average wind speed in Honolulu, Hawaii is 18.2 km/h. Assume that the wind speed is normally distributed with a standard deviation of 5.6 km/h.
 - a. Calculate the probability that the wind speed on any one reading will exceed 26.2 km/h.
 - b. Calculate the probability that the mean of a random sample of 4 readings will exceed 26.2 km/h.
 - c. Calculate the probability that the mean of a random sample of 40 readings will be more than 4 km/h from the expected speed.
 - d. How would your answer in (a), (b), and (c) change if you could not assume that the wind speed in Honolulu is distributed normally?
- B3. When new paperback novels are promoted at bookstores, a display is often arranged with copies of the same book with differently colored covers. A publishing house wanted to find out whether there is dependence between the place where the books is sold and the color of its cover. For one of latest novels, the publisher sent displays and a supply of copies of the novel in a large bookstores in five major cities. The resulting sales of the novel for each city-color combinations are as follows. Numbers are in thousands of copies sold over a 3-month period.

City	Red	Blue	Green	Yellow	Total
New York	21	27	40	15	103
Washington	14	18	28	8	68
Boston	11	13	21	7	52
Chicago	3	33	30	9	75
Los Angeles	30	11	34	10	85
Totals	79	102	153	49	383

Assume that the data are random samples for each particulars color-city combinations and that the inference may apply to all novels. Conduct the overall test for independence of color and location.

SECTION C Compulsary Case Study(15 marks)

Case: Unemployment Study

Each month the U.S. Bureau of Labor Statistics publishes a variety of unemployment statistics, including the number of individuals who are unemployed and the mean length of time the individuals have been unemployed. For November 1998, the Bureau of Labor statistics reported that the national mean length of time of unemployment was 14.6 weeks.

Age	Weeks	Age	Weeks	Age	Weeks	Age	Weeks
56	22	49	26	44	38	27	7
35	19	33	13	27	14	30	10
22	7	56	15	24	6	33	23
57	37	20	17	27	7	32	8
40	18	31	11	45	25	22	7
22	11	27	17	42	33	51	12
48	6	23	3	45	16	50	16
48	22	45	17	44	12	21	9
25	5	29	14	21	13	38	5
40	20	31	4	31	16	26	8
25	12	59	39	42	4	55	35
25	1	39	7	23	14		
59	33	35	12	51	31		

The mayor of Philadelphia requested a study on the status of unemployment in the Philadelphia area. A sample of 50 unemployed residents of Philadelphia included data on there age and the number of weeks without a job. A portion of the data collected in November 1998 follows. The complete data set is available in the data file BLS.

Descriptive statistics to summarize the data.

∤ge		Weeks	
Mean	36.6	Mean	15.54
Median	34	Median	13.5
Mode	27	Mode	7
Sample Variance	142.6939	Sample Variance	98.53918
Kurtosis	-1.14515	Kurtosis	0.053711
Skewness	0.357283	Skewness	0.910766
Range	39	Range	38
Minimum	20	Minimum	1
Maximum	59	Maximum	39
Sum	1830	Sum	777
Count	50	Count	50

Managerial Report

- 1. Develop a 95% confidence interval estimate of the mean age of unemployed individuals in Philadelphia.
- 2. Conduct a hypothesis test to determine whether the mean duration of unemployment in Philadelphia is greater than the national mean duration of 14.6 weeks. Use a .01 level of significance. What is your conclusion?
- 3. Is there a relationship between the age of an unemployed individual and the number of weeks of unemployment? Explain.

Standard Normal Probabilities

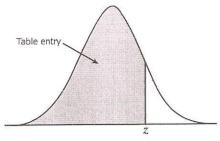


Table entry for z is the area under the standard normal curve to the left of z.

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
0.0	.5000	.5040	.5080	.5120	.5160	.5199	.5239	.5279	.5319	.5359
0.1	.5398	.5438	.5478	.5517	.5557	.5596	.5636	.5675	.5714	.5753
0.2	.5793	.5832	.5871	.5910	.5948	.5987	.6026	.6064	.6103	.6141
0.3	.6179	.6217	.6255	.6293	.6331	.6368	.6406	.6443	.6480	.6517
0.4	.6554	.6591	.6628	.6664	.6700	.6736	.6772	.6808	.6844	.6879
0.5	.6915	.6950	.6985	.7019	.7054	.7088	.7123	.7157	.7190	.7224
0.6	.7257	.7291	.7324	.7357	.7389	.7422	.7454	.7486	.7517	.7549
0.7	.7580	.7611	.7642	.7673	.7704	.7734	.7764	.7794	.7823	.7852
0.8	.7881	.7910	.7939	.7967	.7995	.8023	.8051	.8078	.8106	.8133
0.9	.8159	.8186	.8212	.8238	.8264	.8289	.8315	.8340	.8365	.8389
1.0	.8413	.8438	.8461	.8485	.8508	.8531	.8554	.8577	.8599	.8621
1.1	.8643	.8665	.8686	.8708	.8729	.8749	.8770	.8790	.8810	.8830
1.2	.8849	.8869	.8888	.8907	.8925	.8944	.8962	.8980	.8997	.9015
1.3	.9032	.9049	.9066	.9082	.9099	.9115	.9131	.9147	.9162	.9177
1.4	.9192	.9207	.9222	.9236	.9251	.9265	.9279	.9292	.9306	.9319
1.5	.9332	.9345	.9357	.9370	.9382	.9394	.9406	.9418	.9429	.9441
1.6	.9452	.9463	.9474	.9484	.9495	.9505	.9515	.9525	.9535	.9545
1.7	.9554	.9564	.9573	.9582	.9591	.9599	.9608	.9616	.9625	.9633
1.8	.9641	.9649	.9656	.9664	.9671	.9678	.9686	.9693	.9699	.9706
1.9	.9713	.9719	.9726	.9732	.9738	.9744	.9750	.9756	.9761	.9767
2.0	.9772	.9778	.9783	.9788	.9793	.9798	.9803	.9808	.9812	.9817
2.1	.9821	.9826	.9830	.9834	.9838	.9842	.9846	.9850	.9854	.9857
2.2	.9861	.9864	.9868	.9871	.9875	.9878	.9881	.9884	.9887	.9890
2.3	.9893	.9896	.9898	.9901	.9904	.9906	.9909	.9911	.9913	.9916
2.4	.9918	.9920	.9922	.9925	.9927	.9929	.9931	.9932	.9934	.9936
2.5	.9938	.9940	.9941	.9943	.9945	.9946	.9948	.9949	.9951	.9952
2.6	.9953	.9955	.9956	.9957	.9959	.9960	.9961	.9962	.9963	.9964
2.7	.9965	.9966	.9967	.9968	.9969	.9970	.9971	.9972	,9973	.9974
2.8	.9974	.9975	.9976	.9977	.9977	.9978	.9979	.9979	.9980	.9981
2.9	.9981	.9982	.9982	.9983	.9984	.9984	.9985	.9985	.9986	.9986
3.0	.9987	.9987	.9987	.9988	.9988	.9989	.9989	.9989	.9990	.9990
3.1	.9990	.9991	.9991	.9991	.9992	.9992	.9992	.9992	.9993	.9993
3.2	.9993	.9993	.9994	.9994	.9994	.9994	.9994	.9995	.9995	
3.3	.9995	.9995	.9995	.9996	.9996	.9996	.9996	.9996	.9996	.9997
3.4	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9997	.9998

Standard Normal Probabilities

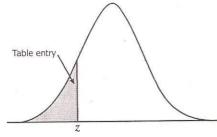
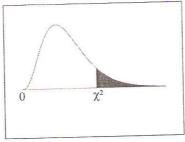


Table entry for \boldsymbol{z} is the area under the standard normal curve to the left of \boldsymbol{z} .

z	.00	.01	.02	.03	.04	.05	.06	.07	.08	.09
-3.4	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0003	.0002
-3.3	.0005	.0005	.0005	.0004	.0004	.0004	.0004	.0004	.0004	.0003
-3.2	.0007	.0007	.0006	,0006	.0006	.0006	.0006	.0005	.0005	.0005
-3.1	.0010	.0009	.0009	.0009	.0008	.0008	.0008	.0008	.0007	.0007
-3.0	.0013	.0013	.0013	.0012	.0012	.0011	.0011	.0011	.0010	.0010
-2.9	.0019	.0018	.0018	.0017	.0016	.0016	.0015	.0015	.0014	.0014
-2.8	.0026	.0025	.0024	.0023	.0023	.0022	.0021	.0021	.0020	.0019
-2.7	.0035	.0034	.0033	.0032	.0031	.0030	.0029	.0028	.0027	.0026
-2.6	.0047	.0045	.0044	.0043	.0041	.0040	.0039	.0038	.0037	.0036
-2.5	.0062	.0060	.0059	.0057	.0055	.0054	.0052	.0051	.0049	.0048
-2.4	.0082	.0080	.0078	.0075	.0073	.0071	.0069	.0068	.0066	.0064
-2.3	.0107	.0104	.0102	.0099	.0096	.0094	.0091	.0089	.0087	.0084
-2.2	.0139	.0136	.0132	.0129	.0125	.0122	.0119	.0116	.0113	.0110
-2.1	.0179	.0174	.0170	.0166	.0162	.0158	.0154	.0150	.0146	.0143
-2.0	.0228	.0222	.0217	.0212	.0207	.0202	.0197	.0192	.0188	.0183
-1.9	.0287	.0281	.0274	.0268	.0262	.0256	.0250	.0244	.0239	.0233
-1.8	.0359	.0351	.0344	.0336	.0329	.0322	.0314	.0307	.0301	.0294
-1.7	.0446	.0436	.0427	.0418	.0409	.0401	.0392	.0384	.0375	.0367
-1.6	.0548	.0537	.0526	.0516	.0505	.0495	.0485	.0475	.0465	.0455
-1.5	.0668	.0655	.0643	.0630	.0618	.0606	.0594	.0582	.0571	.0559
-1.4	.0808	.0793	.0778	.0764	.0749	.0735	.0721	.0708	.0694	.0681
-1.3	.0968	.0951	.0934	.0918	.0901	.0885	.0869	.0853	.0838	.0823
-1.2	.1151	.1131	.1112	.1093	.1075	.1056	.1038	.1020	.1003	.0985
-1.1	.1357	.1335	.1314	.1292	.1271	.1251	.1230	.1210	.1190	.1170
-1.0	.1587	.1562	.1539	.1515	.1492	.1469	.1446	.1423	.1401	.1379
-0.9	.1841	.1814	.1788	.1762	.1736	.1711	.1685	.1660	.1635	.1611
-0.8	.2119	.2090	.2061	.2033	.2005	.1977	.1949	.1922	.1894	.1867
-0.7	.2420	.2389	.2358	.2327	.2296	.2266	.2236	.2206	.2177	.2148
-0.6	.2743	.2709	.2676	.2643	.2611	.2578	.2546	.2514	.2483	.2451
-0.5	.3085	.3050	.3015	.2981	.2946	.2912	.2877	.2843	.2810	.2776
-0.4	.3446	.3409	.3372	.3336	.3300	.3264	.3228	.3192	.3156	.3121
-0.3	.3821	.3783	,3745	.3707	.3669	.3632	.3594	.3557	.3520	.3483
-0.2	.4207	.4168	.4129	.4090	.4052	.4013	.3974	.3936	.3897	.3859
-0.1	.4602	.4562	.4522	.4483	.4443	.4404	.4364	.4325	.4286	.4247
-0.0	.5000	.4960	.4920	.4880	.4840	.4801	.4761	.4721	.4681	.4641

Chi-Square Distribution Table



The shaded area is equal to α for $\chi^2 = \chi^2_{\alpha}$.

df	χ ² _{.995}	X ² _{.990}	χ ² _{.975}	$\chi^{2}_{.950}$	$\chi^{2}_{.900}$	χ ² _{.100}	$\chi^{2}_{.050}$	$\chi^{2}_{.025}$	$\chi^{2}_{.010}$	$\chi^{2}_{.005}$
					0.016	2.706	3.841	5.024	6.635	7.879
1	0.000	0.000	0.001	0.004	0.010	4.605	5.991	7.378	9.210	10.597
2	0.010	0.020	0.051	0.103	0.584	6.251	7.815	9.348	11.345	12.838
3	0.072	0.115	0.216	0.352	1.064	7.779	9.488	11.143	13.277	14.860
4	0.207	0.297	0.484	0.711	1.610	9.236	11.070	12.833	15.086	16.750
5	0.412	0.554	0.831	1.145	2.204	10.645	12.592	14.449	16.812	18.548
6	0.676	0.872	1.237	1.635	2.833	12.017	14.067	16.013	18.475	20.278
7	0.989	1.239	1.690	2.167		13.362	15.507	17.535	20.090	21.955
8	1.344	1.646	2.180	2.733	3.490	14.684	16.919	19.023	21.666	23.589
9	1.735	2.088	2.700	3.325	4.168	15.987	18.307	20.483	23.209	25.188
10	2.156	2.558	3.247	3.940	4.865	17.275	19.675	21.920	24.725	26.757
11	2.603	3.053	3.816	4.575	5.578	The second secon	21.026	23.337	26.217	28.300
12	3.074	3.571	4.404	5.226	6.304	18.549	22.362	24.736	27.688	29.819
13	3.565	4.107	5.009	5.892	7.042	19.812	23.685	26.119	29.141	31.319
14	4.075	4.660	5.629	6.571	7.790	21.064	24.996	27.488	30.578	32.801
15	4.601	5.229	6.262	7.261	8.547	22.307		28.845	32.000	34.267
16	5.142	5.812	6.908	7.962	9.312	23.542	26.296	30.191	33.409	35.718
17	5.697	6.408	7.564	8.672	10.085	24.769	27.587	31.526	34.805	37.156
18	6.265	7.015	8.231	9.390	10.865	25.989	28.869	32.852	36.191	38.582
19	6.844	7.633	8.907	10.117	11.651	27.204	30.144	34.170	37.566	39.997
20	7.434	8.260	9.591	10.851	12.443	28.412	31.410	35.479	38.932	41.401
21	8.034	8.897	10.283	11.591	13.240	29.615	32.671		40.289	42.796
22	8.643	9.542	10.982	12.338	14.041	30.813	33.924	36.781	41.638	44.181
23	9.260	10.196	11.689	13.091	14.848	32.007	35.172	38.076	42.980	45.559
24	9.886	10.856	12.401	13.848	15.659	33.196	36.415	39.364	44.314	46.928
25	10.520	11.524	13.120	14.611	16.473	34.382	37.652	40.646	44.514	48.290
26	11.160	12.198	13.844	15.379	17.292	35.563	38.885	41.923	46.963	49.645
27	11.808	12.879	14.573	16.151	18.114	36.741	40.113	43.195		50.993
28	12.461	13.565	15.308	16.928	18.939	37.916	41.337	44.461	48.278	52.336
29	13.121	14.256	16.047	17.708	19.768	39.087	42.557	45.722	49.588	53.672
30	13.787	14.953	16.791	18.493	20.599	40.256	43.773	46.979	50.892	
	20.707	22.164	24.433	26.509	29.051	51.805	55.758	59.342	63.691	66.766
40	27.991	29.707	32.357	34.764	37.689	63.167	67.505	71.420	76.154	79.490
50	35.534	37.485	40.482	43.188	46.459	74.397	79.082	83.298	88.379	91.952
60	43.275	45.442	48.758	51.739	55.329	85.527	90.531	95.023	100.425	104.215
70	51.172	53.540	57.153	60.391	64.278	96.578	101.879	106.629	112.329	116.321
80	1	61.754	65.647	69.126	73.291	107.565	113.145	118.136	124.116	128.299
90	59.196	70.065	74.222	77.929	82.358	118.498	124.342	129.561	135.807	140.169
100	67.328	10.005	14.444	11.020	1					

CRITICAL VALUES OF F_{.05}



This table shows the 5 percent right-tail critical values of F for the stated degrees of freedom (v).

Denominator					Numerator	Degrees of		17	9	10	12
Degrees of Freedom (v2)	1	2	3	4	5	6	7	8		241.9	243.9
Freedom (2)			245.7	224.6	230.2	234.0	236.8	238.9	240.5 19.38	19.40	19.41
1	161.4	199.5	215.7	19.25	19.30	19.33	19.35	19.37		8.79	8.74
2	18.51	19.00	19.16		9.01	8.94	8.89	8.85	8.81		5.91
3	10.13	9.55	9.28	9.12	6.26	6.16	6.09	6.04	6.00	5.96	4.68
4	7.71	6.94	6.59	6.39		4.95	4.88	4.82	4.77	4.74	
5	6.61	5.79	5.41	5.19	5.05	4.55			4.10	4.06	4.00
2			. 70	4.53	4.39	4.28	4.21	4.15	3.68	3.64	3.57
. 6	5.99	5.14	4.76	4.12	3.97	3.87	3.79	3.73		3.35	3.28
7	5.59	4.74	4.35		3.69	3.58	3.50	3.44	3.39		3.07
8	5.32	4.46	4.07	3.84		3.37	3.29	3.23	3.18	3.14	2.91
9	5.12	4.26	3.86	3.63	3.48	3.22	3.14	3.07	3.02	2.98	2.91
	4.96	4.10	3.71	3.48	3.33	3.22			2.90	2.85	2.79
10	4.50			3,36	3.20	3.09	3.01	2.95		2.75	2.69
11	4.84	3.98	3.59		3.11	3.00	2.91	2.85	2.80		2.60
12	4.75	3.89	3.49	3.26	3.03	2.92	2.83	2.77	2.71	2.67	2.53
13	4.67	3.81	3.41	3.18		2.85	2.76	2.70	2.65	2.60	
14	4.60	3.74	3.34	3.11	2.96		2.71	2.64	2.59	2.54	2.48
	4.54	3.68	3.29	3.06	2.90	2.79			2.54	2.49	2.4
15	4.54			2.01	2.85	2.74	2.66	2.59	2.54	2.45	2.3
16	4.49	3.63	3.24	3.01	2.81	2.70	2.61	2.55	2.49		2.3
17	4.45	3.59	3.20	2.96		2.66	2.58	2.51	2.46	2.41	2.3
	4.41	3.55	3.16	2.93	2.77		2.54	2.48	2.42	2.38	
18	4.38	3.52	3.13	2.90	2.74	2.63	2.51	2.45	2.39	2.35	2.2
19		3.49	3.10	2.87	2.71	2.60	2.31			2.32	2.2
20	4.35				2.68	2.57	2.49	2.42	2.37		2.2
21	4.32	3.47	3.07	2.84	2.66	2.55	2.46	2.40	2.34	2.30	2.2
22	4.30	3.44	3.05	2.82		2.53	2.44	2.37	2.32	2.27	
	4.28	3.42	3.03	2.80	2.64		2.42	2.36	2.30	2.25	2.1
23	4.26	3.40	3.01	2.78	2.62	2.51	2.40	2.34	2.28	2.24	2.
24		3.39	2.99	2.76	2.60	2.49	2.40			2.22	2.
25	4.24	5.55			2.59	2.47	2.39	2.32	2.27		2.
26	4,23	3.37	2.98	2.74		2.46	2.37	2.31	2.25	2.20	
	4.21	3.35	2.96	2.73	2.57		2.36	2.29	2.24	2.19	2.
27	4.20		2.95	2.71	2.56	2.45	2.35			2.18	2.
28				2.70	2.55	2.43				2.16	2.
29	4.18			2.69	2.53	2.42	2.33	2.2.		2.00	2.
30	4.17	5.52			2 45	2.34	2.25	2.18	2.12		
40	4.08	3.23	2.84		2.45				2.07		
	4.03			2.56						1.99	
50	4.00			2.53						1.91	
60					2.29						3 1
120	3.92		하다 보세하는 아픈 중심하게 보였			2.14	2.06				
200	3.89 2.71						2.10	2.01	1.94	1 1.88	\$

Some important Formulae

$$\frac{\overline{X} - \mu}{\sigma / \sqrt{n}} \qquad \frac{\overline{X} - \mu}{s / \sqrt{n}} \qquad \frac{\hat{p} - p}{\sqrt{\frac{p(1 - p)}{n}}}$$

$$\frac{\overline{X} - \mu_0}{\sigma / \sqrt{n}} \qquad \frac{\overline{X} - \mu_0}{s / \sqrt{n}} \qquad \frac{(\hat{p} - p_0)}{\sqrt{\frac{p_0(1 - p_0)}{n}}}$$

$$\begin{array}{lll} \sigma_{\hat{p}} = \sqrt{\frac{pq}{n}} & z = \frac{\hat{p} - p}{\sigma_{\hat{p}}} \\ \bar{x} \pm z \frac{\sigma}{\sqrt{n}} & \bar{x} \pm z \frac{\hat{\sigma}}{\sqrt{n}} \\ \\ \sigma_{\bar{p}_1 - \bar{p}_2} = \sqrt{\frac{p_1 q_1}{n_1} + \frac{p_2 q_2}{n_2}} \\ s_p^2 = \frac{(n_1 - 1)s_1^2 + (n_2 - 1)s_2^2}{n_1 + n_2 - 2} \\ \\ \chi^2 \left(\text{df} \left(r \text{-} 1 \right)^* (\text{c-} 1) \right) = \sum_i \frac{(O_i - E_i)^2}{E_i} \\ \\ \text{SSB} = \sum_{i=1}^k n_i (\bar{x}_i - \bar{\bar{x}})^2 & \text{d.f.} = \text{k-} 1 \\ \text{SST} = \sum_{i=1}^k \sum_{j=1}^{n_i} (x_{ij} - \bar{\bar{x}})^2 & \text{d.f.} = \text{n-} 1 \\ \\ \text{MSB} = \frac{SSB}{k - 1} \\ \text{F} \left(\text{k-} 1 \right), (\text{n-k}) & \text{d.f.} = \frac{MSB}{MSW} \\ \end{array} \right.$$

$$s_{b_1} = \frac{s}{\sqrt{\sum (x_i - \overline{x})^2}}$$

$$b_1 \pm t_{\alpha/2} s_{b_1}$$

$$b_1 = \frac{\sum (x - \overline{x})(y - \overline{y})}{\sum (x - \overline{x})^2}$$
2 SSR regression sum of square

$$r^{2} = \frac{SSR}{SST} = \frac{regression sum of squares}{total sum of squares}$$

$$\begin{aligned} & \mathsf{FPCF} = \sqrt{\frac{N-n}{N-1}} \\ \bar{x} \pm t \frac{\hat{\sigma}}{\sqrt{n}} & \bar{p} \pm z \hat{\sigma_{\bar{p}}} \\ & \sigma_{\bar{x_1} - \bar{x_2}} = \sqrt{\frac{\hat{\sigma_1}^2}{n_1} + \frac{\hat{\sigma_2}^2}{n_2}} \\ & t = \frac{\bar{x_1} - \bar{x_2} - (\mu_1 - \mu_2)}{\sigma_{\bar{x_1} - \bar{x_2}}} \end{aligned}$$

$$SSW = \sum_{i=1}^{k} \sum_{j=1}^{n_i} (X_{ij} - \bar{x_i})^2 \quad \text{d.f.} = \text{n-k}$$

$$SST = SSB + SSW \quad SSW \text{ is also written as SSE}$$

$$MSW \text{ (or MSE)} = \frac{SSW}{n-k}$$

$$s = \sqrt{MSE} = \sqrt{\frac{SSE}{n-2}}$$

$$\hat{y}_1 = b_0 + b_1 x$$

$$b_0 = \overline{y} - b_1 \overline{x}$$